

- NB 1) Q1 is compulsory.
2) Attempt any **three** questions from remaining questions
3) Assume suitable data wherever required.

- Q1) a) Sketch the signal $x(t) = 2u(t) + tu(t) - (t-1)u(t-1) - 3u(t-2)$ [5*4]
b) State and prove Parseval's theorem for non-periodic signals.
c) Find the Z transform of the given function
 $x(n) = (1/4)^n u(n) + (1/5)^n u(-n-1)$
d) Compute DFT of the given sequence $x(n) = \{0,1,2,3\}$

- Q2) a) Determine the inverse Z-transform

$$H(Z) = \frac{(Z-1)(Z+2)}{(Z-\frac{1}{2})(Z-\frac{3}{4})} \quad \text{ROC: } |Z| > \frac{3}{4} \quad [05]$$

- b) Find the initial value and final value of

$$X(Z) = \frac{Z}{4Z^2 - 5Z - 1} \quad \text{ROC: } |Z| > 1 \quad [05]$$

- c) An LTI system is described by $2y(n) + 3y(n-1) + y(n-2) = u(n) + u(n-1) - u(n-2)$. Find the response of the system when initial conditions are given $y(-1) = 2$, $y(-2) = -1$ and unit step is applied at the input. [10]

- Q3) a) Show pole Zero diagram of the given transfer function

$$h(n) = (0.5)^n \quad 0 \leq n \leq 7 \quad [10]$$

- b) The difference equation of the system is given as $y(n) = 2x(n) + x(n-1)$. Find the magnitude and phase response. [10]

- Q4) a) Classify the following systems as linear, non-linear, time-variant, time invariant, causal, non-causal, static; dynamic, stable and unstable. [10]

a) $y(n) = n x(n)$ b) $y(t) = x(t^2)$

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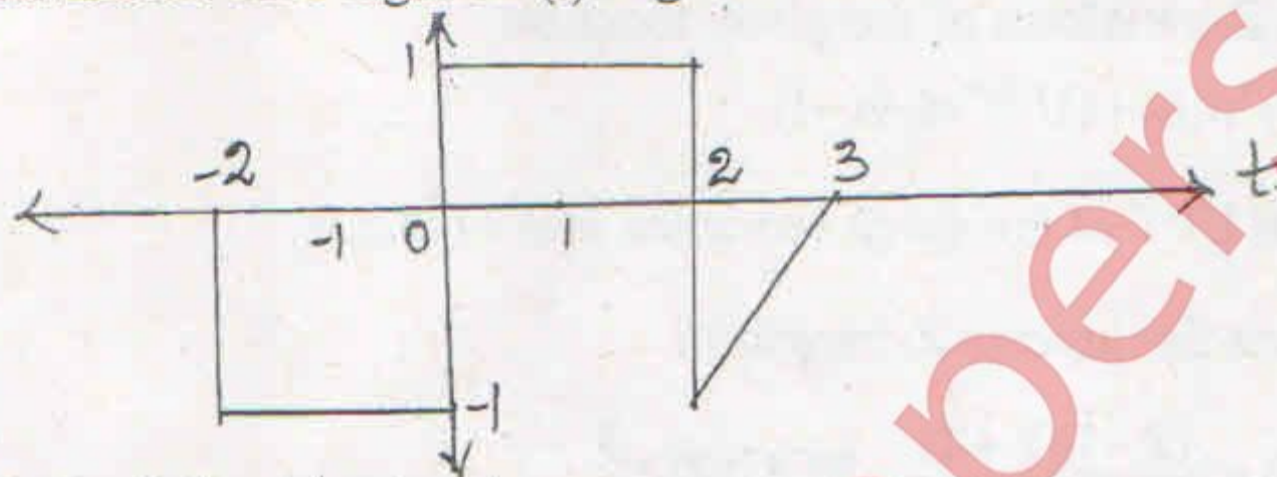
b) Find the inverse z-transform of the $X(z) = \frac{z}{3z^2 - 4z + 1}$ for the following ROC conditions: 1) $|z| > 1$ 2) $|z| < 1/3$ 3) $1/3 < |z| < 1$ [10]

Q5) Obtain the magnitude and phase response of the following system by Analytical and Geometric method:

$$h(n) = \{1, 1/2\}$$

[10]

b) A continuous time signal $x(t)$ is given below: [10]



Sketch the following signals:

a) $x_1(t) = x(-t)$ b) $x_2(t) = -2x(t)$ c) $x_3(t) = x(t-3) - 2x(t)$ d) $x_4(t) = x(t/2)$

Q6) a) An 8 point sequence is given by $X(n) = \{2, 2, 2, 2, 1, 1, 1, 1\}$. Compute 8 point DFT of $x(n)$ by radix-2 DIT-FFT method. [10]

b) Prove any four DFT properties [10]